KANGAROO MATH THAILAND

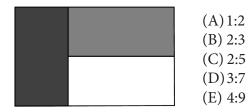
student

STUDENT PROBLEM

KANGAROO MATH THAILAND 2019

3 points

#1. The flag of Kangoraland is a rectangle which is divided into three smaller equal rectangles as shown. What is the ratio of the side lengths of the white rectangle?

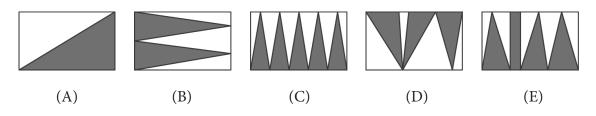


#2. The numbers 1, 2, 3 and 4 are each written in different cells of the 2×2 table. After that, the sum of the numbers in each row and column is calculated. Two of these sums are 4 and 5. What are the other two sums?



- (A) 6 and 6
- (B) 3 and 5
- (C) 4 and 5
- (D) 4 and 6
- (E) 5 and 6

#3. A rectangle has been shaded in five different ways as shown. In which diagram does the shaded part have the largest area?



#4. Three triangles are linked as shown. Which of the following pictures shows these three triangles linked in the same way?





(B)



(C)

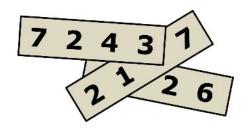




#5. A pyramid has 23 triangular faces. How many edges does this pyramid have?

- (A) 23
- (B) 24
- (C) 46
- (D) 48
- (E) 69

#6. Three 4-digit numbers are written on three pieces of paper as shown. The sum of the three numbers is 11126. Three of the digits are covered. What are the covered digits?



- (A) 1, 4 and 7
- (B) 1, 5 and 7
- (C) 3, 3 and 3
- (D) 4, 5 and 6
- (E) 4, 5 and 7

#7. What is the first (leftmost) digit of the smallest positive integer whose digits add up to 2019?

- (A) 2
- (B) 3
- (C) 4
- (D) 5
- (E) 6

#8. Each of the faces of a die is marked with either 1, 2 or 3 dots so that the probability of rolling a 1 is $\frac{1}{2}$, the probability of rolling a 2 is $\frac{1}{3}$ and the probability of rolling a 3 is $\frac{1}{6}$. Which of the following cannot be a view of this die?







(B)





(D)



(E)

#9. Michael invented a new " \Diamond " operation for real numbers, defined as $x\Diamond y = y - x$. If a, b, and c satisfy $(a \lozenge b) \lozenge c = a \lozenge (b \lozenge c)$, which of the following statements is necessarily true?

- (A) a = b
- (B) b = c
- (C) a = c
- (D) a = 0
- (E) c = 0

#10. How many of the numbers from 2^{10} to 2^{13} , inclusive, are divisible by 2^{10} ?

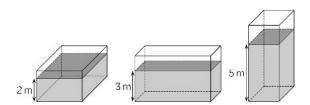
- (A) 2
- (B) 4
- (C) 6
- (D) 8
- (E) 16

4 points

#11. Which is the highest power of 3 dividing the number 7!+8!+9! ?

- (A) 3^2
- (B) 3^4
- (C) 3⁵
- (D) 3^6
- (E) a power of 3 higher than 3⁶

- #12. This year, the number of boys in my class has increased by 20% and the number of girls has decreased by 20%. We now have one student more than before. Which of the following could be the number of students in my class now?
 - (A) 22
- (B) 26
- (C) 29
- (D) 31
- (E) 34
- #13. A container in the shape of a rectangular box is partially filled with 120 m³ of water. The depth of the water is either 2 m or 3 m or 5 m, depending on which side of the box is on the ground, as shown (not to scale). What is the volume of the container?

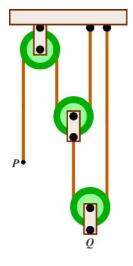


- (A) 160 m^3
- (B) 180 m^3
- $(C) 200 \text{ m}^3$
- (D) 220 m^3
- (E) 240 m^3
- #14. Three kangaroos, Alex, Bob and Carl, go for a walk every day. If Alex doesn't wear a hat, then Bob wears a hat. If Bob doesn't wear a hat, then Carl wears a hat. Today Carl is not wearing a hat. Who is certainly wearing a hat today?
 - (A) only Alex and Bob
- (D) neither Alex nor Bob

(B) only Alex

- (E) only Bob
- (C) Alex, Bob and Carl
- #15. The system shown consists of three pulleys with vertical sections of rope between them.

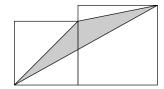
 The end P is moved down 24 centimeters. How many centimeters does point Q move up?



- (A) 24
- (B) 12
- (C) 8
- (D)6
- (E) $\frac{24}{5}$

- #16. A positive integer n is called good if its largest divisor (excluding *n*) is equal to *n*-6. How many good positive integers are there?
 - (A) 1
- (B) 2
- (C) 3
- (D) 6
- (E) infinitely many
- #17. A box contains 4 chocolates and 1 fruit chew. John and Mary take turns drawing a treat out of the box without replacement. Whoever draws the fruit chew wins. John draws first. What is the probability that Mary wins?

- (A) $\frac{2}{5}$ (B) $\frac{3}{5}$ (C) $\frac{1}{2}$ (D) $\frac{5}{6}$ (E) $\frac{1}{3}$
- #18. Two adjacent squares with side lengths a and b (a < b) are shown. What is the area of the shaded triangle?



- (A) \sqrt{ab} (B) $\frac{1}{2}a^2$ (C) $\frac{1}{2}b^2$ (D) $\frac{1}{4}(a^2+b^2)$ (E) $\frac{1}{2}(a^2+b^2)$
- #19. What is the integer part of $\sqrt{20 + \sqrt{20 + \sqrt{20 + \sqrt{20} + \sqrt{20}}}}$?
 - (A) 4
- (B) 5
- (C)6
- (D) 20
- (E) 25
- #20. To calculate the result of $\frac{a+b}{c}$, Sara types $a+b \div c = \text{ on a calculator and the result is } 11$ (a, b, and c are positive integers). She then types $b+a \div c=$ and she is surprised to see that the result is 14. She realizes that the calculator is designed to calculate divisions before additions. What is the correct result of $\frac{a+b}{c}$?
 - (A) 1
- (B) 2
- (C) 3
- (D) 4
- (E) 5

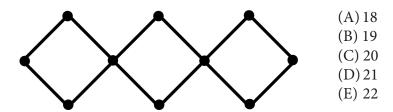
5 points

- #21. Let a be the sum of all positive divisors of 1024 and b the product of all positive divisors of 1024. Then
 - (A) $(a-1)^5=b$
- (B) $(a+1)^5=b$ (C) $a^5=b$

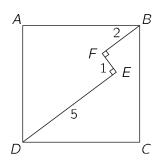
- (D) $a^5-1=b$ (E) $a^5+1=b$
- #22. What is the set of all values of the parameter a for which the number of solutions of the equation 2-|x|=ax is equal to two?
 - (A) $(-\infty, -1)$ (B) (-1, 1)
- (C) $[1, +\infty)$
- $(D) \{0\}$
- $(E) \{-1, 1\}$

KSF 2019 - Problems Student

#23. The vertices of the network shown are labelled with the numbers from 1 to 10. The sum S of the four labels on each square is the same. What is the least possible value of S?



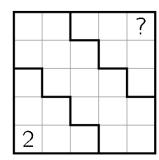
- #24. How many planes pass through at least three vertices of a given cube?
 - (A) 6
- (B) 8
- (C) 12
- (D) 16
- (E) 20
- #25. Four distinct straight lines pass through the origin of the coordinate system. They intersect the parabola $y = x^2 - 2$ at eight points. What can be the product of the *x*-coordinates of these eight points?
 - (A) Only 16
- (B) Only -16
- (C) Only 8
- (D) Only -8
- (E) There are several possible
- #26. For how many integers n is $\lfloor n^2 2n 3 \rfloor$ a prime number?
 - (A) 1
- (B) 2
- (C) 3
- (D) 4
- (E) infinitely many
- #27. A path DEFB with DE \perp EF and EF \perp FB lies inside the square ABCD as shown. Given that DE=5, EF=1 and FB=2, what is the length of the side of the square?



- (A) $3\sqrt{2}$
- (B) $\frac{7\sqrt{2}}{2}$ (C) $\frac{11}{2}$ (D) $5\sqrt{2}$
- (E) none of the previous

- #28. The sequence a^1 , a^2 , a^3 , ... starts with $a^1=49$. For $n\ge 1$, the number a_{n+1} is obtained by adding 1 to the sum of the digits of a_n and then squaring the result. Thus $a_2 = (4+9+1)^2 = 196$. Determine a_{2019} .
 - (A) 121
- (B) 25
- (C) 64
- (D) 400
- (E) 49
- #29. Three different numbers are chosen at random from the set $\{1,2,3,\ldots,10\}$. What is the probability that one of them is the average of the other two?
 - (A) $\frac{1}{10}$ (B) $\frac{1}{6}$ (C) $\frac{1}{4}$ (D) $\frac{1}{3}$ (E) $\frac{1}{2}$

- #30. The square shown is filled with numbers in such a way that each row and each column contains the numbers 1,2,3,4 and 5 exactly once. Moreover, the sum of the numbers in each of the three bold-bordered areas is equal. What number is in the upper right corner?



- (A) 1
- (B) 2
- (C)3
- (D)4
- (E) 5



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